



## Method of designs

- Allowable Strength Design (ASD)
- Load and Resistance Factor Design (LRFD)
- Both procedures are based on limit states design principles.
- Limit states is used to describe a condition at which a structure or part of a structure would be stopped to perform its function.
- - **Strength**: define load carrying capacity, including (excessive yielding, fracture, buckling, fatigue, and gross rigid body motion).
- - **Serviceability**: define the performance including (deflection, cracking, slipping, vibration, and deterioration).
- All limit states must be prevented.



### ◆ Allowable Strength Design (ASD)

required strength  $\leq$  allowable strength

Largest computed force in member  $\rightarrow$

$$R_a \leq \frac{R_n}{\Omega}$$

Required Strength (ASD)  $\uparrow$   $\leftarrow$  Nominal Strength  $\leftarrow$  Factor of Safety

### ◆ Load and Resistance Factor Design (LRFD)

required strength  $\leq$  design strength

Load factor  $> 1$

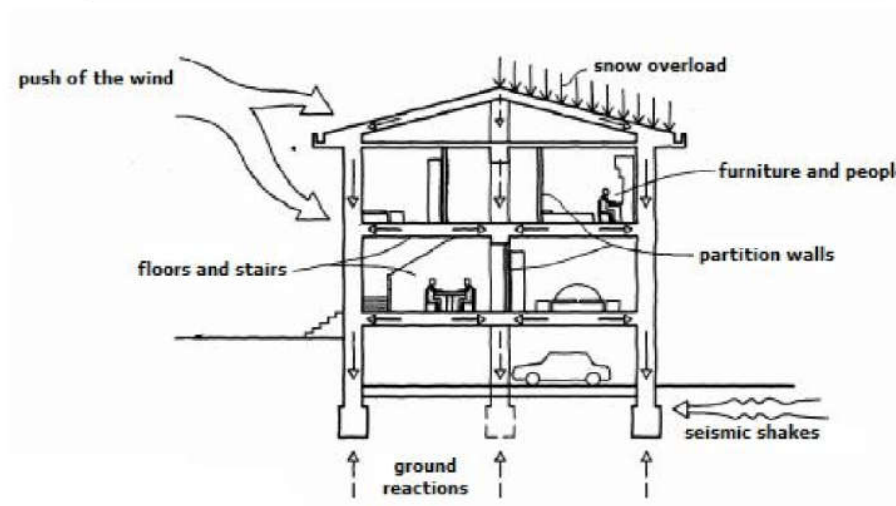
$$R_u = \sum \gamma_i Q_{ni} \leq \phi R_n$$

Required Strength (LRFD)  $\uparrow$   $\leftarrow$  Load  $\leftarrow$  Resistance Factor  $< 1$   $\leftarrow$  Nominal Strength/Resistance

## ASD Load Combinations

1.  $D$
2.  $D + L$
3.  $D + (L_r \text{ or } S \text{ or } R)$
4.  $D + 0.75L + 0.75(L_r \text{ or } S \text{ or } R)$
5.  $D + (0.6W \text{ or } 0.7E)$
6.  $D + 0.75L \pm 0.75(0.6W) + 0.75(L_r \text{ or } S \text{ or } R)$
7.  $D + 0.75L \pm 0.75(0.7E) + 0.75S$
8.  $0.6D \pm 0.6W$  UPLIFT
9.  $0.6D \pm 0.7E$  UPLIFT

## Possible Loads



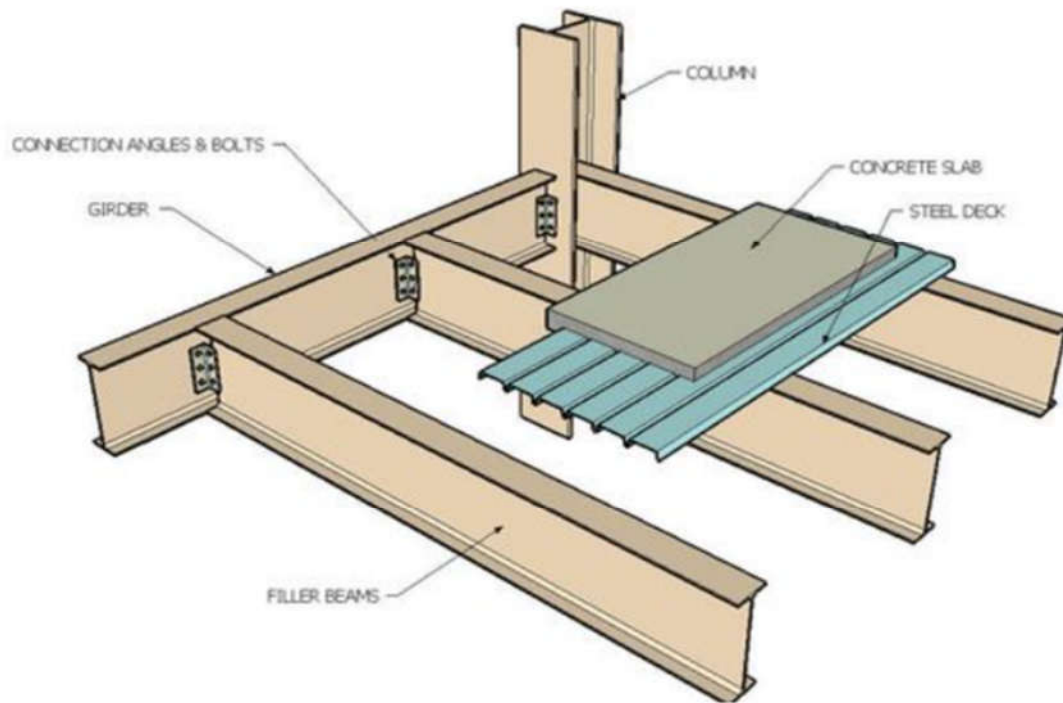


## LRFD Load Combinations

1.  $1.4D$
2.  $1.2D + 1.6L + 0.5(L_r \text{ or } S \text{ or } R)$
3.  $1.2D + 1.6(L_r \text{ or } S \text{ or } R) + (0.5L \text{ or } 0.5W)$
4.  $1.2D \pm 1.0W + 0.5L + 0.5(L_r \text{ or } S \text{ or } R)$
5.  $1.2D \pm 1.0E + 0.5L + 0.2S$
6.  $0.9D \pm 1.0W$  UPLIFT
7.  $0.9D \pm 1.0E$  UPLIFT

Note: The load factor on  $L$  in load combinations 3, 4 and 5 is taken as 1.0 if the service live load is greater than 100 psf, and 0.5 for all other cases

## Load path



### Load path for gravity loads:

1. floor slab (metal deck + concrete) → beams
2. beams → girders
3. girders → columns



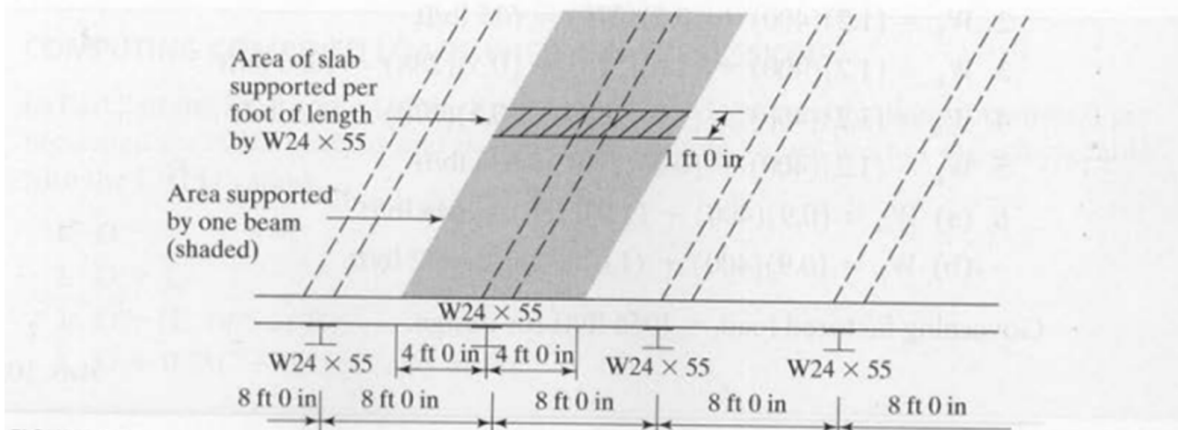
### Example 2-1

The interior floor system shown in Figure 2.2 has W24 × 55 sections spaced 8 ft on center and is supporting a floor dead load of 50 psf and a live floor load of 80 psf. Determine the governing load in lb/ft that each beam must support.

**Solution.** Note that each foot of the beam must support itself (a dead load) plus  $8 \times 1 = 8 \text{ ft}^2$  of the building floor.

$$D = 55 \text{ lb/ft} + (8 \text{ ft})(50 \text{ psf}) = 455 \text{ lb/ft}$$

$$L = (8 \text{ ft})(80 \text{ psf}) = 640 \text{ lb/ft}$$



Computing factored loads, using the LRFD load combinations. In this substitution, the terms having no values are omitted. Note that with a floor live load of 80 psf a load factor of 0.5 has been added to load combinations (3.), (4.), and (5.) per the exception stated in ASCE 7-10 and this text for floor live loads.

1.  $W_u = (1.4)(455) = 637 \text{ lb/ft}$
2.  $W_u = (1.2)(455) + (1.6)(640) = 1570 \text{ lb/ft}$
3.  $W_u = (1.2)(455) + (0.5)(640) = 866 \text{ lb/ft}$
4.  $W_u = (1.2)(455) + (0.5)(640) = 866 \text{ lb/ft}$
5.  $W_u = (1.2)(455) + (0.5)(640) = 866 \text{ lb/ft}$
6.  $W_u = (0.9)(455) = 409.5 \text{ lb/ft}$
7.  $W_u = (0.9)(455) = 409.5 \text{ lb/ft}$

Governing factored load = 1570 lb/ft to be used for design.



## Acceptable level of safety

$$R_a \leq \frac{R_n}{\Omega}$$

$$R_u = \sum \gamma_i Q_{ni} \leq \phi R_n$$

$$\Omega = 1.5 / \phi$$

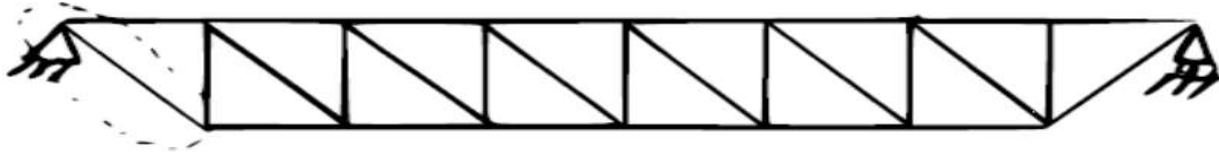
$$\text{IF } \phi = 0.9 \longrightarrow \Omega = 1.67$$

$$\text{IF } \phi = 0.75 \longrightarrow \Omega = 2.00$$

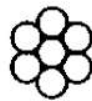


## Tension Members

- Found in bridge, roof trusses, towers, bracing systems, and used as a tie rods.



Bars  
(round and rectangular)



Cables



Single and double angles

A few examples of shapes typically used for tension members





## Limit States in Tension



gross-section yield



net-section fracture



block shear fracture

### Gross-section yield

$$P_n = F_y A_g$$

Equation D2-1

$$\phi_t = 0.90 \quad (\Omega_t = 1.67)$$

$A_g$  = Gross Area  
Total cross-sectional area in the plane perpendicular to tensile stresses.



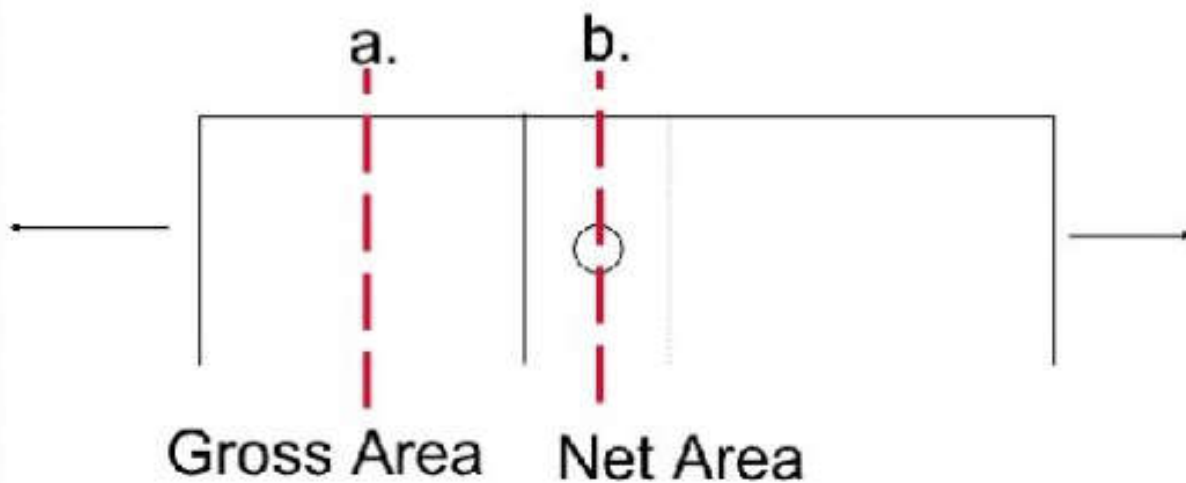


## Net-section fracture

$$P_n = F_u A_e \quad \text{Equation D2-2}$$

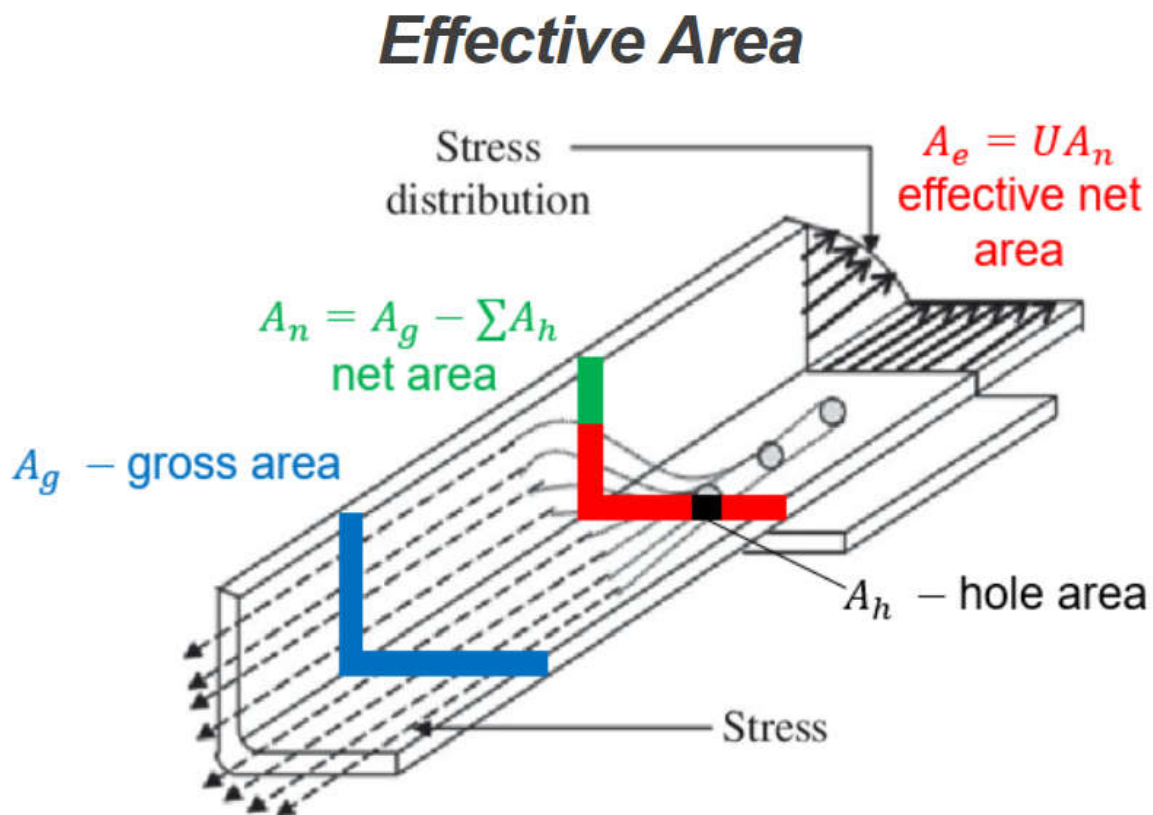
$$\phi_t = 0.75 \quad (\Omega_t = 2.00)$$

$A_e$  = Effective Net Area  
Accounts for any holes or openings, potential failure planes not perpendicular to the tensile stresses, and effects of shear lag.



## Shear lag factor (U)

- The factor, U, is used to account for the effects of shear lag, which is a reduction in the effective area of a cross section as the stress flows from a uniform distribution in the member to a more concentrated distribution in the vicinity of connections that do not engage the full cross section for force transfer.





**Part 16 (Specifications)**  
**Chapter D**

**TABLE D3.1**  
**Shear Lag Factors for Connections**  
**to Tension Members**

Case	Description of Element	Shear Lag Factor, $U$	Example
1	All tension members where the tension load is transmitted directly to each of cross-sectional elements by fasteners or welds. (except as in Cases 3, 4, 5 and 6)	$U = 1.0$	
2	All tension members, except plates and HSS, where the tension load is transmitted to some but not all of the cross-sectional elements by fasteners or longitudinal welds (Alternatively, for W, M, S and HP, Case 7 may be used.)	$U = 1 - \bar{x}/l$	
3	All tension members where the tension load is transmitted by transverse welds to some but not all of the cross-sectional elements.	$U = 1.0$ and $A_n$ = area of the directly connected elements	
4	Plates where the tension load is transmitted by longitudinal welds only.	$l \geq 2w \dots U = 1.0$ $2w > l \geq 1.5w \dots U = 0.87$	



Shape	Gross Area, $A_g$  in. <sup>2</sup>	$A_e =$ $0.75A_g$  in. <sup>2</sup>	Yielding		Rupture		
			kips		kips		
			$P_n/\Omega_t$	$\phi_t P_n$	$P_n/\Omega_t$	$\phi_t P_n$	
			ASD	LRFD	ASD	LRFD	
L8×8×1 1/8	16.7	12.5	360	541	363	544	
	×1	15.0	11.3	323	486	328	492
	×7/8	13.2	9.90	285	428	287	431
	×3/4	11.4	8.55	246	369	248	372
	×5/8	9.61	7.21	207	311	209	314
	×9/16	8.68	6.51	187	281	189	283
	×1/2	7.75	5.81	167	251	168	253
L8×6×1	13.0	9.75	280	421	283	424	
	×7/8	11.5	8.63	248	373	250	375
	×3/4	9.94	7.46	214	322	216	325
	×5/8	8.36	6.27	180	271	182	273
	×9/16	7.56	5.67	163	245	164	247
	×1/2	6.75	5.06	146	219	147	220
	×7/16	5.93	4.45	128	192	129	194



## Example

Determine the net area of the  $3/8 \times 8$  in plate as shown below. The plate is connected at its end with two lines of  $3/4$  in bolts.

