

Bias Stabilization

Basic Definitions

The stability of system is a measure of sensitivity of a circuit to variations in its parameters. In any amplifier employing a transistor the **collector current I_C** is sensitive to each of the following parameter.

- **I_{CO} (reverse saturation current): doubles in value for every 10°C increase in temperature**
- **$|V_{BE}|$ (base-to-emitter voltage): decrease about 7.5 mV per 1°C increase in temperature.**
- **β (forward current gain): increase with increase in temperature.**

Any or all of these factors can cause the bias point to drift from the design point of operation.

Stability Factors, $S(I_{CO})$, $S(V_{BE})$, and $S(\beta)$:

A stability factor, S , is defined for each of the parameters affecting bias stability as listed below:

$$S_{I_{CO}} = \frac{\Delta I_C}{\Delta I_{CO}} \frac{\partial I_C}{\partial I_{CO}} \bigg|_{V_{BE}, \beta \text{ const.}} \quad [10.1a]$$

$$S_{V_{BE}} = \frac{\Delta I_C}{\Delta V_{BE}} \frac{\partial I_C}{\partial V_{BE}} \bigg|_{V_{BE}, \beta \text{ const.}} \quad [10.1b]$$

$$S_{\beta} = \frac{\Delta I_C}{\Delta \beta} \frac{\partial I_C}{\partial \beta} \bigg|_{V_{BE}, I_{CO} \text{ const.}} \quad [10.1c]$$

Generally, networks that are quite stable and relatively insensitive to temperature variations have low stability factors. In some ways it would seem more appropriate to consider the quantities defined by Eqs. [10.1a - 10.1c] to be sensitivity factors because:

the higher the stability factor, the more sensitive the network to variations in that parameter.

The total effect on the collector current can be determined using the following equation:

$$\Delta I_C \approx S_{I_{CO}} \Delta I_{CO} + S_{V_{BE}} \Delta V_{BE} + S_{\beta} \Delta \beta \quad [10.2]$$

Derivation of Stability Factors for Standard Bias Circuits:

For the **voltage-divider bias circuit**, the exact analysis (using Thevenin theorem) for the input (base-emitter) loop will result in

$$E_{Th} - I_B R_B - V_{BE} - I_E R_E = 0$$

$$I_E = I_C \approx I_B$$

$$I_C R_E \approx I_B (R_E + R_{Th}) \approx V_{BE} + E_{Th}$$

$$I_C \approx \beta I_B \approx \beta (1 + \beta) I_{co}$$

$$I_B \approx \frac{I_C}{\beta} = \frac{1 + \beta}{\beta} I_{co} \Rightarrow$$

$$I_C \approx \frac{\beta (1 + \beta) R_E + R_{Th}}{\beta} I_{co} + \frac{V_{BE} + E_{Th}}{\beta} \quad [10.3]$$

The partial derivation of the Eq. [10.3] with respect to I_{CO} will result:

$$\frac{\partial I_C}{\partial I_{CO}} \cdot \frac{\beta (1 + \beta) R_E + R_{Th}}{\beta} = 1 + \frac{\beta (1 + \beta) R_E + R_{Th}}{\beta} = 0$$

$$S = \frac{R}{\beta (1 + \beta) R_E + R_{Th}} \quad [10.4a]$$

Also, the partial derivation of the Eq. [10.3] with respect to V_{BE} will result:

$$\frac{\partial I_C}{\partial V_{BE}} \cdot \frac{\beta (1 + \beta) R_E + R_{Th}}{\beta} = 1 = 0$$

$$S_{V_{BE}} = \frac{-\beta}{\beta + 1 + R_E/R_{Th}}$$

[10.4b]

The mathematical development of the last stability factor $S(\beta)$ is more complex than encountered for $S(I_{CO})$ and $S(V_{BE})$. Thus, $S(\beta)$ is suggested by the following equation:

$$S_{\beta} = \frac{R_{Th} + R_E}{R_{Th} + R_E + \beta R_E} \left(1 + \frac{R_E}{R_{Th}} \right) \left(1 + \frac{R_E}{R_{Th}} \right) \left(1 + \frac{R_E}{R_{Th}} \right)$$

[10.4c]

For the **emitter-stabilized bias circuit**, the stability factors are the same as these obtained above for the voltage-divider bias circuit except that R_{Th} will be replaced by R_B .

These are:

$$S_{I_{CO}} = \frac{R}{R + \beta R_E + R_B}$$

[10.5a]

$$S_{V_{BE}} = \frac{-\beta}{\beta R_E + R_B}$$

[10.5b]

$$S_{I_{C1}} = \frac{R}{R + \beta_1 R_E + R_B} \left(\beta_1 + \beta_2 \frac{R_E}{R_B} \right)$$

[10.5c]

For the **fixed-bias circuit**, if we plug in $R_E = 0$ the following equation will result:

$$S_{I_{CO}} = \beta + 1$$

[10.6a]

$$S_{V_{BE}} = \frac{-\beta}{R_B}$$

[10.6b]

$$S_{I_{C1}} = \beta \frac{I_{C1}}{\beta_1}$$

[10.6c]

Finally, for the case of the **voltage-feedback bias circuit**, the following equation will result:

$$S_{I_{CO}} = \frac{R + \beta R_E}{R + \beta R_E + R_B}$$

$$\begin{aligned}
 & R_C \parallel R \\
 & R_C \parallel R \\
 & \beta \parallel 1 \parallel \frac{E \parallel R_B}{s I_{CO} \parallel \beta}
 \end{aligned}
 \tag{10.7a}$$

$$\begin{aligned}
 & R_C \parallel R \\
 & \beta \parallel 1 \parallel \frac{E \parallel R_B}{s V_{BE} \parallel \beta}
 \end{aligned}
 \tag{10.7b}$$

$$\begin{aligned}
 & R_C \parallel R \\
 & I_{C1} \parallel \beta_1 \parallel \frac{E \parallel R_B}{s \beta \parallel \beta_2 \parallel 1 \parallel R_C \parallel R_E \parallel R_B}
 \end{aligned}
 \tag{10.7c}$$

Example 10-1:

1. Design a voltage-divider bias circuit using a V_{CC} supply of +18 V, and an npn silicon transistor with β of 80. Choose $R_C = 5R_E$, and set I_C at 1 mA and the stability factor $S(I_{CO})$ at 3.8.
2. For the circuit designed in part (1), determine the change in I_C if a change in operating conditions results in I_{CO} increasing from 0.2 to 10 μA , V_{BE} drops from 0.7 to 0.5 V, and β increases 25%.
3. Calculate the change in I_C from 25 $^{\circ}$ C to 75 $^{\circ}$ C for the same circuit designed in part (1), if $I_{CO} = 0.2 \mu A$ and $V_{BE} = 0.7 V$.

Solution:

Part 1:

$$V_{CE} = V_{CC} - I_C R_C - I_E R_E \approx 2 \times 18 - 2 \times 9 V.$$

$$V_{CE} = V_{CC} - I_C R_C - I_E R_E, R_C = 5 R_E \Rightarrow$$

$$9 = 18 - 1 m \times 5 R_E - 1 m \times R_E \Rightarrow R_E = 1.5 k \Omega$$

$$R_C = 5 \times 1.5 k \Omega = 7.5 k \Omega.$$

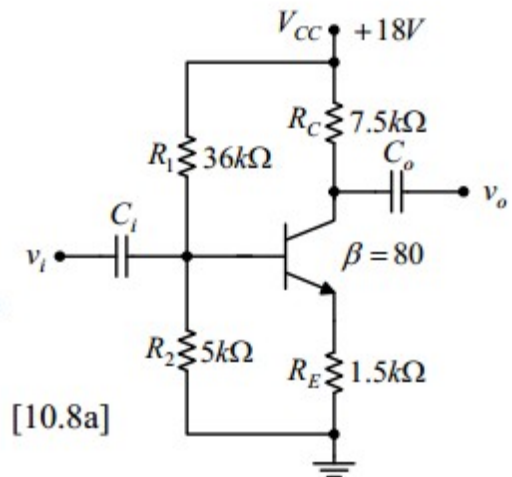
$$I_E \approx I_C = 1 mA, V_E = I_E R_E = 1 m \times 1.5 k \Omega = 1.5 V.$$

$$V_B = \frac{R_2 V_{CC}}{R_1 + R_2} \Rightarrow \frac{R_2}{R_1 + R_2} = \frac{V_B}{V_{CC}} = \frac{2.2}{18}$$

$$S = \beta + 1 \left(\frac{R_E + R_{Th}}{\beta R_E + R_{Th}} \right)$$

$$3.8 = \frac{81 \times (1.5 k + R_{Th})}{81 \times 1.5 k + R_{Th}} \Rightarrow R_{Th} = 4.4 k \Omega$$

$$R_{Th} = \frac{R_1 R_2}{R_1 + R_2} \Rightarrow \frac{R_2}{R_1 + R_2} = \frac{R_{Th}}{R_1} = \frac{4.4 k}{R_1}$$



[10.8a]

[10.8a]

Fig. 10-1

From Eqs. [10.8a] and [10.8b]:

$$\frac{4.4k}{R_1} \approx \frac{2.2}{18} \Rightarrow R_1 \approx 36k \Omega.$$

From Eq. [10.8a]:

$$\frac{R_2}{36k \approx R_2} \approx \frac{2.2}{18} \Rightarrow R_2 \approx 5k \Omega.$$

Fig. 10-1 shows the final circuit.

Part 2:

$$S \uparrow I_{CO} \approx 3.8,$$

$$\Delta I_{CO} \approx 10 \mu - 0.2 \mu \approx 9.8 \mu A$$

$$S \uparrow V_{BE} \approx \frac{-\beta}{\beta \approx 1 \parallel R_E \approx R_{Th}} \approx \frac{-80}{81 \parallel 1.5k \parallel 4.4k} \approx -0.635 mS$$

$$\Delta V_{BE} \approx 0.5 - 0.7 \approx -0.2 V.$$

$$\beta_2 \approx \beta_1 \uparrow 1 \approx 25 \rightarrow 100 \approx 1.25 \beta_1 \approx 1.25 \uparrow 80 \approx 100,$$

$$\begin{aligned} & \frac{R}{1m} \\ & \frac{80 \parallel 1.5k \parallel 4.4k}{101 \parallel 1.5k \parallel 4.4k} \approx 0.473 \mu A, \\ & I_{C1} \approx \beta_1 \parallel \frac{E \approx R_{Th}}{\beta_2 \approx 1 \parallel R_E \approx R_{Th}} \approx \beta_1 \parallel \frac{E \approx R_{Th}}{\beta_2 \approx 1 \parallel R_E \approx R_{Th}} \\ & s \uparrow \beta \approx \uparrow \end{aligned}$$

$$\Delta \beta \approx 100 - 80 \approx 20.$$

$$\Delta I_C \approx S \uparrow I_{CO} \parallel \Delta I_{CO} \approx S \uparrow V_{BE} \parallel \Delta V_{BE} \approx s \uparrow \beta \parallel \Delta \beta$$

$$\uparrow 3.8 \parallel 9.8 \mu \parallel -0.635 m \parallel -0.2 \parallel 0.473 \mu \parallel 20 \approx 0.174 mA$$

Part 3:

Since I_{CO} , doubles in value for every 10°C increase in temperature.

$$\text{Thus } N \approx \frac{\Delta T}{10} \approx \frac{75-25}{10} \approx 5, I_{CO} \uparrow 75^\circ C \approx 2^N \cdot I_{CO} \uparrow 25^\circ C \approx 2^5 \parallel 0.2 \mu \approx 6.4 \mu A$$

$$\Delta I_{CO} \approx 6.4 \mu - 0.2 \mu \approx 6.2 \mu A.$$

Since V_{BE} , decreases about 7.5 mV per 1°C increase in temperature.

Thus $\Delta T \approx 75 - 25 \approx 50^\circ C, V_{BE} \approx 25^\circ C \approx 0.7 V.$

$$V_{BE} \approx 75^\circ C \approx 0.7 - 50 \times 7.5 m \approx 0.325 V.$$

$$\Delta I_C \approx S I_{CO} \Delta I_{CO} \approx S V_{BE} \Delta V_{BE}$$

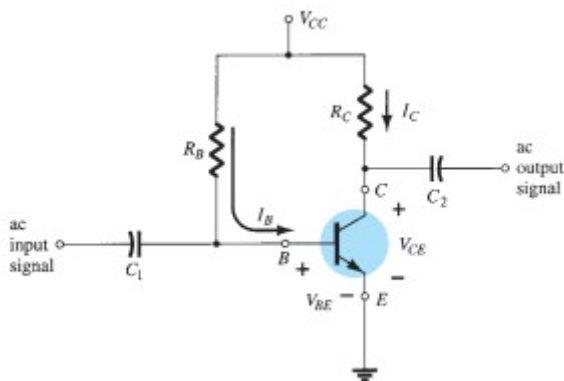
$$\approx 3.8 \times 6.2 \mu \approx -0.635 m \approx -0.375 \approx 0.262 mA.$$

Techniques of stabilizations:

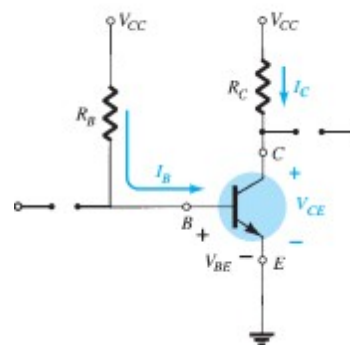
1. Stabilization technique , these use sensitive biasing circuits which allows I_B to vary so as to keep I_C relating constant with variation in $I_{CO}, \beta, \Delta V_{BE}.$
2. Compensation techniques: These use temperature sensitive devices like diodes, transistor, thermistor for providing compensating voltage and current to maintain Q-point constant.

Bias stabilization techniques:

1-Fixed-Bias circuit.



fixed-bias circuit



DC-equivalent of fixed-bias circuit

$$V_{CC} - I_B R_B - V_{BE} = 0$$

$$I_B = \frac{V_{CC} - V_{BE}}{R_B}$$

$$I_C = \beta I_B$$

$$V_{CE} = I_C R_C - V_{CC} = 0$$

$$V_{CE} = V_{CC} - I_C R_C$$

$$\therefore V_{CE} = V_{CC}$$

In addition since $V_{BE} = V_B - V_E \Rightarrow V_{BE} = V_B$

Note:

$$I_E = I_C + I_B, I_C = \beta I_B$$

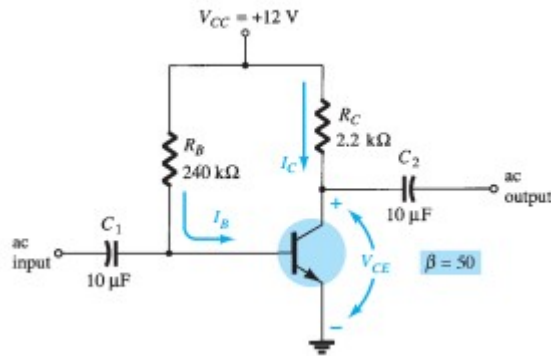
$$I_E = (1 + \beta) I_B$$

$$I_E = I_C$$

Example:

Determine the following for the fixed-bias configuration of Fig. below.

- a) I_{BQ} and I_{CQ} b) V_{CEQ} c) V_B and V_C d) V_{BC}



Solution:

a) $I_{BQ} = \frac{V_{CC} - V_{BE}}{R_B} = \frac{12 - 0.7}{240k} = 47.08 \mu A$

$I_{CQ} = \beta I_B = 50 \times 47.08 \mu A = 2.35 \text{ mA}$

b) $V_{CEQ} = V_{CC} - I_C R_C$
 $= 12 - (2.35 \text{ mA}) \times (2.2 \text{ k}\Omega)$
 $= 6.83 \text{ V}$

c) $V_{BC} = V_B - V_C = 0.7 - 6.83 = -6.13 \text{ V}$

The negative sign revealing the junction is reversed biased as it should be for linear amplification.

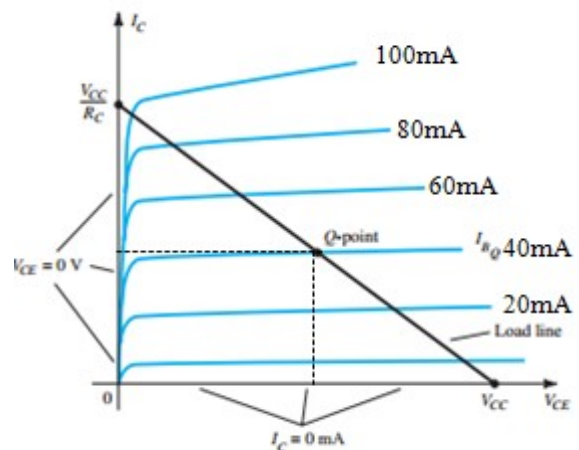
$V_{CE} = V_{CC} - I_C R_C$

but $V_{CE} = 0$

$I_C = I_{C,sat} = \frac{V_{CC}}{R_C}$, at $V_{CE} = 0$

$V_{CE} = V_{CC} - I_C R_C$

$V_{CE} = V_{CC}$, at $I_C = 0$

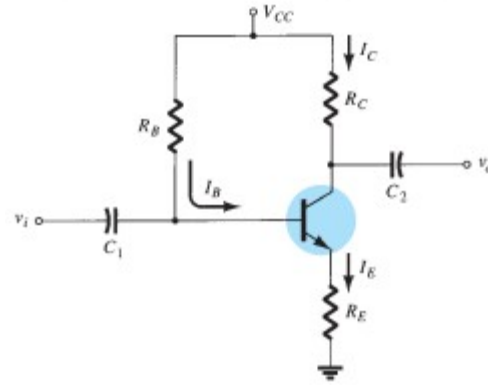


2- Emitter-Stabilized Bias circuit.

$$V_{CC} - I_B R_B - V_{BE} - I_E R_E = 0$$

$$I_E \approx (\beta + 1) I_B$$

$$I_B = \frac{V_{CC} - V_{BE}}{R_B + (\beta + 1) R_E}$$



$$I_E \approx I_C$$

$$R = R_B + (\beta + 1) R_E$$

$$C = R_E$$

$$V_{CE} = V_{CC} - I_C R_C$$

$$V_E = I_E R_E$$

$$V_{CE} = V_{CC} - V_E = V_{CC} - I_E R_E$$

$$\therefore V_{CE} = V_{CC} - I_C R_C$$

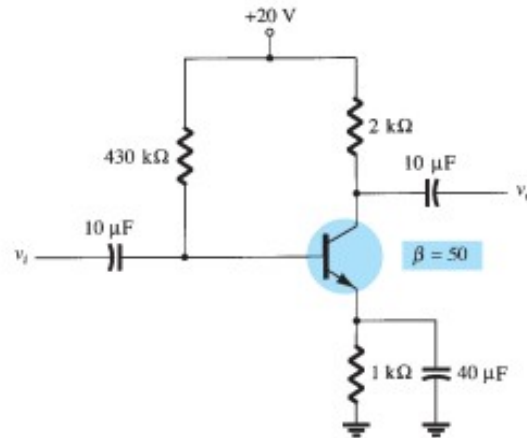
$$V_B = V_{BE} + V_E$$

$$V_B = V_{CC} - I_B R_B$$

Example:

Determine the following for the emitter-bias configuration of Fig. below.

- a) I_B b) I_C c) V_{CE} d) V_C e) V_E f) V_B g) V_{BC}



a) $I_B = \frac{V_{CC} - V_{BE}}{R_B + \beta + 1 R_E}$

$= \frac{20 - 0.7}{430k + 51 \cdot 1k} = 40.1 \mu A$

b) $I_C = \beta I_B = 50 \cdot 40.1 \mu A = 2.01 mA$

c) $V_{CE} = V_{CC} - I_C R_C - I_C R_E$

$= 20 - 2.01 mA \cdot 2k - 2.01 mA \cdot 1k = 13.97 V$

d) $V_C = V_{CC} - I_C R_C = 20 - 2.01 mA \cdot 2k = 15.98 V$

e) $V_E = I_E R_E \cong I_C R_E = 2.01 mA \cdot 1k = 2.01 V$

Or $V_E \approx V_C - V_{cE} \approx 15.98 - 13.97 \approx 2.01 V$ |

1) $V_B \approx V_E \approx V_{BE} \approx 2.01 \approx 0.7 \approx 2.71 V$

2) $V_{BC} \approx V_B - V_C \approx 2.71 - 15.98 \approx -13.27 V$

reverse-bias a required

Saturation Level

The collector saturation level or maximum collector current can be determined by :
 Apply a short circuit between the collector–emitter terminals .

$$V_{CE} = V_{CC} - I_C (R_C + R_E)$$

$$I_{sat} = \frac{V_{CC}}{R_C + R_E}$$

Load-line analysis

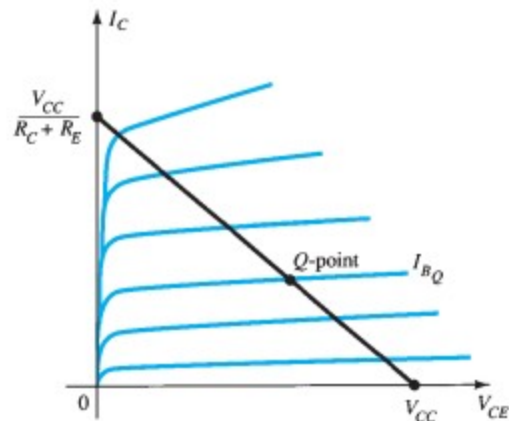
$$V_{CE} = V_{CC} - I_C (R_C + R_E)$$

Choosing $I_C = 0 \text{ mA}$

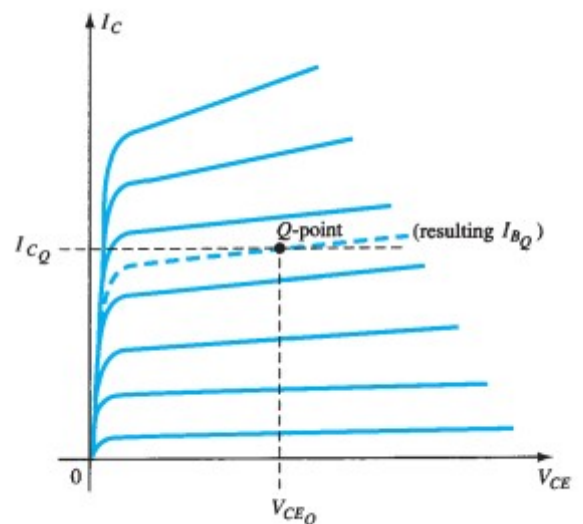
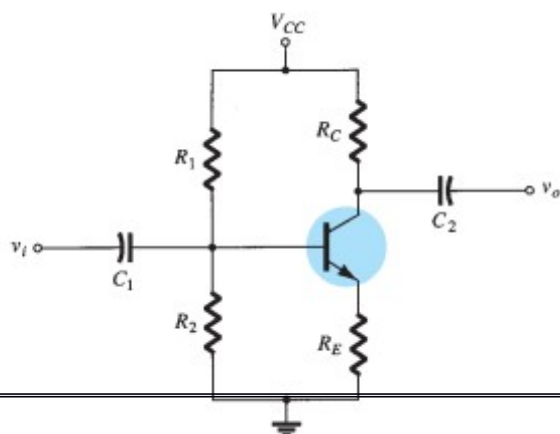
$$V_{CE} = V_{CC}, \text{ at } I_C = 0$$

Choosing $V_{CE} = 0$

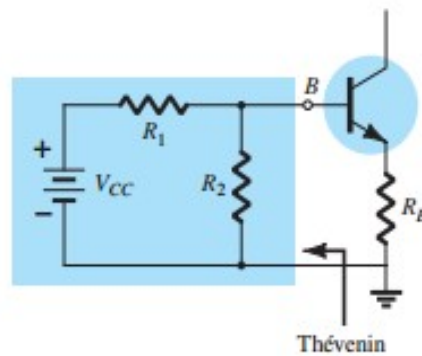
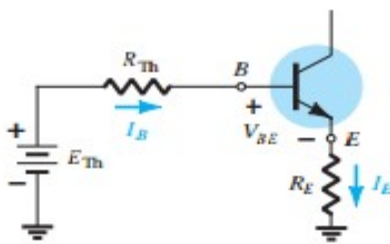
$$I_C = \frac{V_{CC}}{R_C + R_E}, \text{ at } V_{CE} = 0$$



3-Voltage-Divider Bias



$$R_{Th} = R_1 \parallel R_2$$



$$E_{Th} = V_{R_2} = \frac{R_2 V_{CC}}{R_1 + R_2}$$

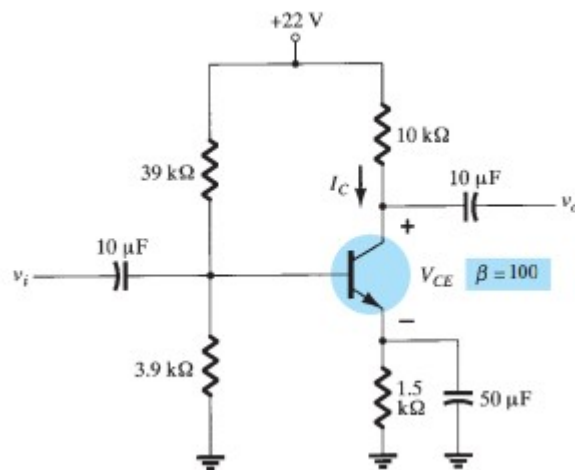
$$E_{Th} - I_B R_{Th} - V_{BE} - I_E R_E = 0$$

$$I_B = \frac{E_{Th} - V_{BE}}{R_{Th} + (\beta + 1) R_E}$$

$$V_{CE} = V_{CC} - I_C R_C$$

Example :

Determine the dc bias voltage V_{CE} and the current I_C for the voltage divider configuration



Solution:

Exact :

$$R_{Th} = R_1 \parallel R_2 = 39k \parallel 3.9k = 3.555 \Omega$$

$$E_{Th} = \frac{R_2 V_{CC}}{R_1 + R_2} = \frac{3.9k \cdot 22V}{39k + 3.9k} = 2V$$

$$I_B = \frac{E_{Th} - V_{BE}}{R_{Th} + \beta + 1 R_E} = \frac{2 - 0.7}{3.55k + 141 + 1.5k} = 6.05 \mu A$$

$$I_{CQ} = \beta I_B = 140 \cdot 6.05 \mu A = 0.85 mA$$

$$V_{CEQ} = V_{CC} - I_C R_E$$

Approximate Analysis:

$$V_B = \frac{R_2 V_{CC}}{R_1 + R_2} \text{ if } R_1 \ll \beta + 1 R_E \approx \beta R_E$$

$$\text{then } \beta R_E \geq 10 R_2$$

$$V_E = V_B - V_{BE}$$

$$I_E = \frac{V_E}{R_E}, I_{CQ} = I_E, V_{CEQ} = V_{CC} - I_C R_E$$

Load-Line Analysis:

$$I_C = \frac{V_{CC}}{R_C + R_E}, \text{ at } V_{CE} = 0$$

$$V_{CE} \approx V_{CC}, \text{ at } I_C \approx 0$$

Example:

Repeat the analysis of last example using the approximate technique, and compare solutions I_{CQ} for and V_{CEQ} .

Solution:

$$\text{Testing: } \beta R_E \geq 10 R_2$$

$$(140)(1.5k) \geq 10(3.9k)$$

$$210k\Omega > 39k\Omega$$

$$V_B \approx \frac{R_2 V_{CC}}{R_1 + R_2} = \frac{3.9k(22)}{39k + 3.9k} \approx 2V$$

$$V_E \approx V_B - V_{BE} = 2 - 0.7 = 1.3V$$

$$I_{CQ} \approx I_E \approx \frac{V_E}{R_E} = \frac{1.3}{1.5k} \approx 0.867mA$$

$$V_{CEQ} \approx V_{CC} - I_C R_C - I_E R_E$$

$$= 22 - (0.85mA)(10k) - (0.85mA)(1.5k)$$

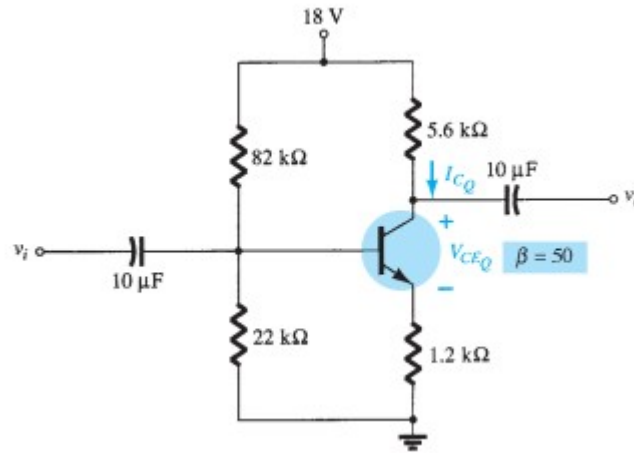
$$= 12.23V$$

Home work:

Repeat the exact analysis of example if $\beta = 70$ and compare solution for I_{CQ} and V_{CEQ} .

Example:

Determine the levels of I_{CQ} and V_{CEQ} for the voltage-divider configuration using the exact and approximate techniques and compare solutions.



Solution:

Exact analysis

$$\beta R_E \geq 10 R_2$$

$$(50)(1.2k) \geq 10 \cdot 22k \quad \text{not satisfied}$$

60k Ω \neq 220k Ω not satisfied

$$R_{Th} = R_1 \parallel R_2 = 82k \parallel 22k = 17.35k \Omega$$

$$E_{Th} = \frac{R_2 V_{CC}}{R_1 + R_2} = \frac{22k \cdot 18V}{82k + 22k} = 3.81V$$

$$I_B = \frac{E_{Th} - V_{BE}}{R_{Th} + \beta R_E} = \frac{3.81V - 0.7V}{17.35k + 50 \cdot 1.2k} = 39.6 \mu A$$

$$I_{CQ} = \beta I_B = 50 \cdot 39.6 \mu A = 1.98 mA$$

$$V_{CEQ} = V_{CC} - I_{CQ} R_C - I_{EQ} R_E$$

Approximate Analysis:

$$V_B = E_{Th} = 3.81V$$

$$V_E = V_B - V_{BE} = 3.81 - 0.7 = 3.11 \text{ V}$$

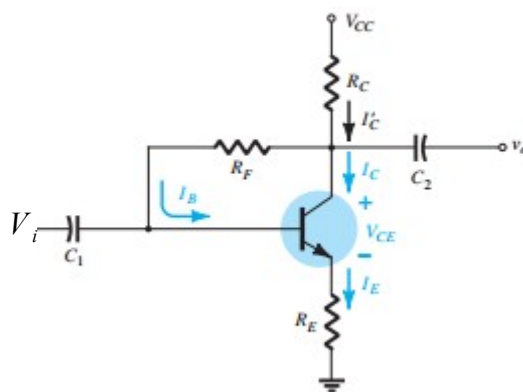
$$I_{CQ} = I_E = \frac{V_E}{R_E} = \frac{3.11}{1.2 \text{ k}} = 2.59 \text{ mA}$$

$$V_{CEQ} = V_{CC} - I_C R_C - I_E R_E = 18 - 2.59 \text{ mA} (5.6 \text{ k} + 1.2 \text{ k}) = 3.88 \text{ V}$$

Tabulating the results, we have:

	I_{CQ}	V_{CEQ}
Exact	1.98	4.
Approximate	2.59	54
		3.
		88

DC Bias with Voltage Feedback:



$$\beta I_B + I_C - I_E = 0$$

$$V_{CC} - I_C R_C - I_E R_E - V_{BE} - I_B R_B = 0$$



$$I_B = \frac{V_{CC} - V_{BE}}{R_B + \beta + 1 R_E}$$

$$I_B = \frac{V'}{R_B + \beta R' + R_E}$$

$$V' = V_{CC} - V_{BE}$$

$$I_B = \frac{V'}{R_B + \beta R'} \quad I_{CQ} = \beta I_B$$

$$I_{CQ} = \frac{\beta V'}{R_B + \beta R'} \cong \frac{\beta V'}{\beta R'} = \frac{V'}{R'} \text{ if } \beta R' \gg R_B$$

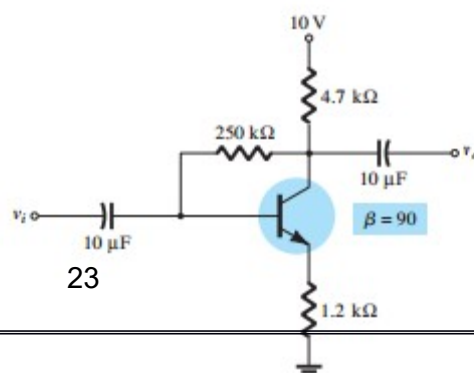
$$I_E R_E = V_{CE} - I_C R_C - V_{CC} = 0$$

$$I_C \cong I_E = I_C$$

$$V_{CE} = V_{CC} - I_C R_C$$

Example:

Determine the quiescent levels of I_{CQ} and V_{CEQ} .



Solution:

$$I_B = \frac{V_{CC} - V_{BE}}{R_B + \beta(1 + R_E)} = \frac{10 - 0.7}{250k + 90(4.7k + 1.2k)} = \frac{9.3V}{250 + 531} = 11.91 \mu A$$

$$I_{CQ} = \beta I_B = 90 \times 11.94 = 1.07 mA$$

$$V_C = I_C R_C + I_E R_E = 1.07 mA (4.7k + 1.2k) = 3.69 V$$

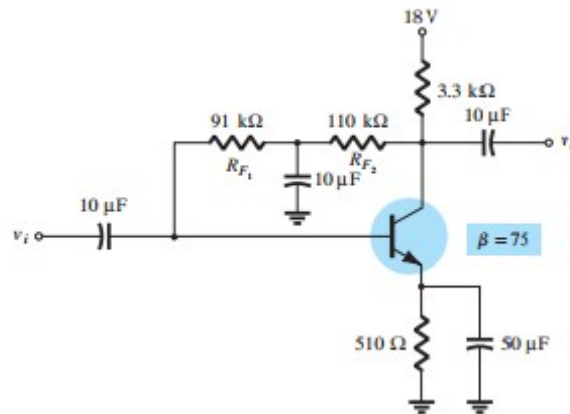
$$V_{CE} = V_{CC} - I_C R_C$$

Home work:

Repeat last example if $\beta = 135$.

Example:

Determine the DC level of I_{CQ} and V_{CEQ}



Solution:

$$R_B = R_{F1} \parallel R_{F2} = 91 \text{ k} \parallel 110 \text{ k} = 51 \text{ k}$$

$$I_B = \frac{V_{CC} - V_{BE}}{R_B + \beta R_E} = \frac{18 - 0.7}{51 \text{ k} + 75 \times 0.51 \text{ k}} = 35.5 \mu\text{A}$$

$$I_{CQ} = \beta I_B = 75 \times 35.5 \mu\text{A} = 2.66 \text{ mA}$$

$$V_{CE} = V_{CC} - I_C R_C \cong V_{CC} - I_C R_C$$

$$V_{CEQ} = 18 - 2.66 \text{ mA} \times 3.3 \text{ k} = 18 - 8.78 = 9.22 \text{ V}$$

Saturation Conditions

$$I_{C \text{ sat}} = I_{C \text{ max}} = \frac{V_{CC}}{R_C + R_E}$$

Collector and base current :

1- Combination current:

$$I_B = I_E - I_C$$

$$I'_B = I'_E - I'_C$$

$$I_C = \alpha I_E$$

$$I'_C = \alpha I'_E$$

$$\text{then } I_B = (1 - \alpha) I_E \quad I'_B = (1 - \alpha) I'_E$$

Reverse leakage current:

$$I_B = I_{CO} + I'_B = I_{CO} + (1 - \alpha) I'_E$$

Then $I'_E = \frac{I_B - I_{CO}}{1 - \alpha}$

$$I_C = \alpha_{dc} I'_E = I_{CO}$$

Then $I_B = \alpha \frac{I_B - I_{CO}}{1 - \alpha} + I_{CO}$

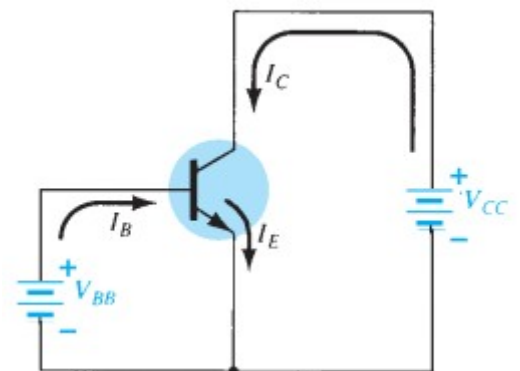
$$\frac{\alpha}{1 - \alpha} I_B = \frac{\alpha}{1 - \alpha} I_{CO} + I_{CO}$$

$$\frac{\alpha}{1 - \alpha} I_B = \frac{\alpha}{1 - \alpha} I_{CO}$$

$$\beta = \frac{\alpha}{1 - \alpha}, \quad \alpha = \frac{\beta}{1 + \beta} \quad \text{then } 1 + \beta = \frac{\beta}{\alpha}$$

$$1 - \alpha = \frac{\alpha}{\beta} \quad \frac{1}{1 - \alpha} = \frac{\beta}{\alpha} \quad 1 + \beta = \beta$$

$$I_C = \beta I_B + (1 + \beta) I_{CO}$$



Stability factor(s)

It is ratio of rate of change of I_C with respect to the reverse saturation current, keeping β and V_{BE} constant

$$S_{I_{CO}} = \frac{\partial I_C}{\partial I_{CO}} \bigg|_{V_{BE}, \beta \text{ constant}} \cong \frac{\Delta I_C}{\Delta I_{CO}}$$

Other stability factors may be defined as

$$S_{\beta} = \frac{\partial I_C}{\partial \beta} \cong \frac{\Delta I_C}{\Delta \beta}$$

$$S_{V_{BE}} = \frac{\partial I_C}{\partial V_{BE}} \bigg|_{\beta, I_{CO} \text{ constant}} \cong \frac{\Delta I_C}{\Delta V_{BE}}$$

$I_C \cong \beta I_B \cong (1 + \beta) I_{CO}$ differentiating with I_C

$$1 + \beta \frac{d I_{CO}}{d I_C} \cong \beta \frac{d I_B}{d I_C}$$

$$1 + \beta \frac{d I_{CO}}{d I_C} \cong \beta \frac{d I_B}{d I_C} \Rightarrow S_{I_{CO}} = \frac{1 + \beta}{1 \pm \beta} \frac{d I_B}{d I_C}$$

For the fixed bias $\Rightarrow I_B \cong \frac{V_{CC} \cdot d I_B}{R_b} \cong 0$

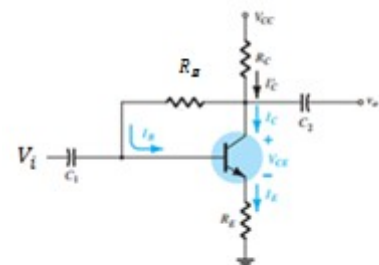
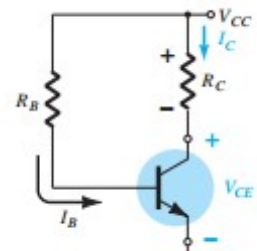
$$S_{I_{CO}} = \frac{1 + \beta}{1 - \beta} \frac{d I_B}{d I_C} \cong \frac{1 + \beta}{1 - 0} \cong 1 + \beta$$

For $\beta \cong 50 \Rightarrow S_{I_{CO}} \cong 1 + 50 \cong 51$

It means that for this circuit I_C increase 51 times as fast as I_{CO}

Networks that are quite stable and relatively insensitive to temperature variations have low stability factor.

How to reduce (S)



In the figure. If $I_C \uparrow$ (due to $\uparrow T \Rightarrow \beta \uparrow$), then $V_{CE} \downarrow$

And hence $I_B \downarrow$ and so also $I_C \downarrow$ and is not allowed to

Exceed as in fixed bias case.

$$-V_{CC} = I_B R_C + I_C R_C + I_B R_B + V_{BE} \quad (1)$$

$$I_B = \frac{V_{CC} - I_C R_C - V_{BE}}{R_C + R_B}$$

Then $\frac{\partial I_B}{\partial I_C} = \frac{-R_C}{R_C + R_B}$

$$S = \frac{1 + \beta}{1 + \beta \frac{R_C}{R_C + R_B}} \therefore S = \beta + 1$$

which is obtained for fixed bias

Minimum value of $S > 0$

Stabilization with change in β

$$-V_{CC} = I_B R_C + I_C R_C + I_B R_B + V_{BE} \quad (1)$$

$$I_C = (1 + \beta) I_B \quad (2)$$

from these two equation.

$$I_C = \frac{\beta V_{CC} - V_{BE} + R_C + R_B}{\beta R_C + R_B} I_{CO}$$

1- To reduce I_C insensitive to β , we must $\beta R_C \gg R_B$ then

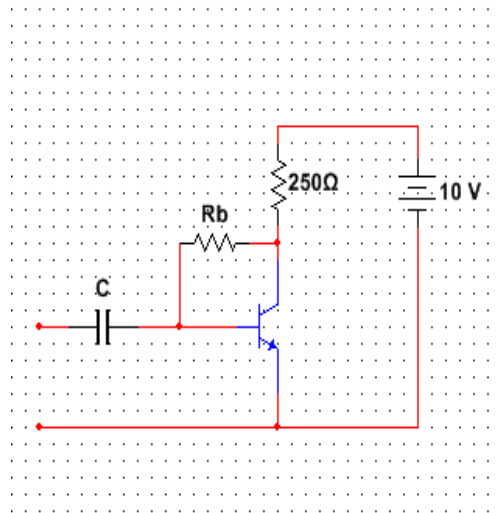
$$I_C \cong \frac{1}{R_C} (V_{CC} - V_{BE} + R_C + R_B) I_{CO}$$

2- If $R_B \gg \beta R_C$, then sensitivity to variation in β is $\frac{1}{2}$ to what it would be, if fixed bias is used,

So feedback resistance R_B increases stability but the voltage gain of the amplifier is reduced.

Example:

Given $\beta = 50$, Q at the middle of load line find R_b & S



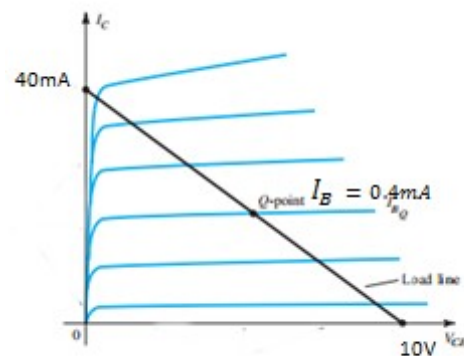
Solution:

$$I_C = \frac{V_{CC}}{R_C} = \frac{10}{250} = 40 \text{ mA}$$

$$I_B = 0.4 \text{ mA}$$

$$I_C = 20 \text{ mA} \quad \left| \text{for } Q \text{ at middle of load line} \right.$$

$$V_C = 5 \text{ V}$$



$$R_b = \frac{V_{CC} - V_{BE}}{I_B} = \frac{5 - 0.6}{0.4} = 11 \text{ k}\Omega \Rightarrow R_b = \frac{V_C - V_B}{I_B}$$

$$S = \frac{1 + \beta}{1 + \beta \frac{R_C}{R_C + R_b}} = \frac{1 + 50}{1 + 50 \frac{0.25}{0.25 + 11}} = 22$$

But βR_C should be $\gg R_b$ to avoid sensitivity of I_C, β

$$\beta R_C = 50 \times 0.25 = 12.5 \text{ k}\Omega$$

$$R_b = 11 \text{ k}\Omega$$

So this condition is not satisfied.

Self Bias or Emitter Bias

By thevenin's equivalent

$$R_b \approx R_1 \parallel R_2$$

If $R_b \rightarrow 0$, then V_{BN} is independent of I_{CO} and hence

$$S \approx \frac{\partial I_C}{\partial I_{CO}} \rightarrow 1$$

For best stability $R_1 \circ R_2$ should be as small as possible.

$$V_{Th} \approx \frac{R_2 V_{CC}}{R_1 + R_2} \quad \text{and} \quad R_b \approx \frac{R_1 R_2}{R_1 + R_2}$$

$$V_{Th} \approx I_B R_b \approx V_{BE} \approx I_B \approx I_C \approx R_e$$

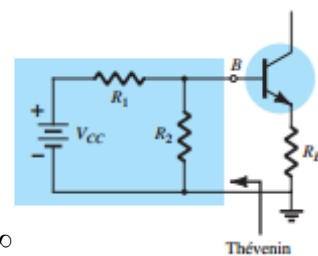
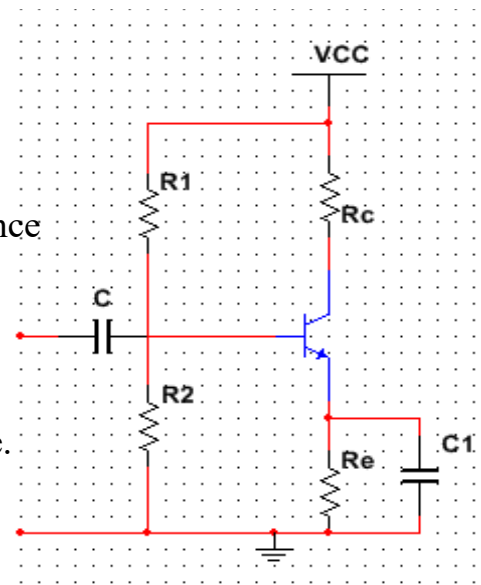
$$\frac{\partial I_B}{\partial I_C} \approx \frac{-R_e}{R_e + R_b}$$

$$S \approx \frac{1 + \beta}{1 - \beta} \frac{\partial I_B}{\partial I_C} \approx \frac{1 + \beta}{1 - \beta} \frac{1 + \frac{R_b}{R_e}}{1 + \frac{R_b}{R_e} + \beta} R_b \approx R_{Th}$$

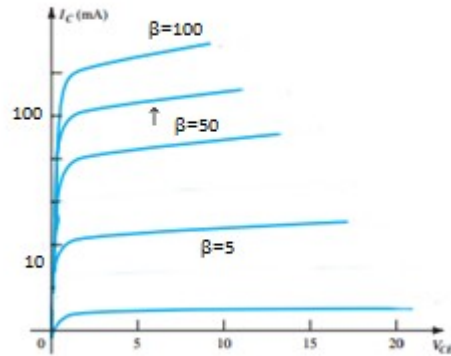
S varies between 1 for small $\frac{R_b}{R_e}$ and $1 + \beta$ for $\frac{R_b}{R_e} \rightarrow \infty$

$S \uparrow$, so $\beta \uparrow$ it is independent of β stability decreases.

For small S, it is independent of β

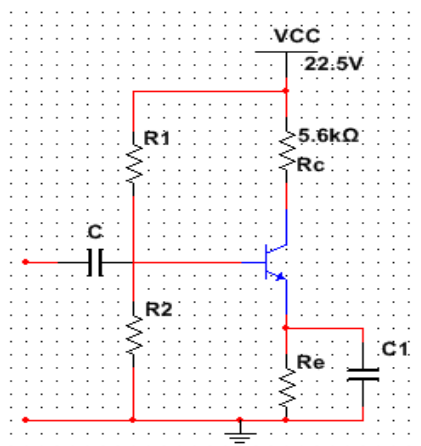


Also a capacitance $C \approx 10 \mu F$ is used to by pass R_e to avoid the loss of AC signal.



Example:

Given $\beta = 50$, $V_{BE} = 0.6 V$, $V_{CC} = 22.5 V$ Q-point at $V_{CE} = 12 V, I_C = 1.5 mA \leq 3$, find R_e , R_1 and R_2



Solution:

$$I_C R_C = V_{CE} - I_C R_e \Rightarrow I_C = \frac{V_{CE}}{R_C + R_e} \Rightarrow I_B = \frac{I_C}{\beta} \Rightarrow V_{BE} = V_{CC} - I_B R_1 - I_C R_C$$

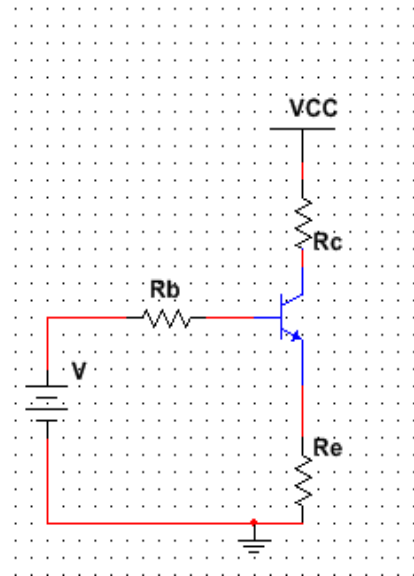
If $I_C \gg I_B$

$$I_C R_C \approx R_e \approx V_{CC} - V_{BE}$$

$$R_C \approx R_e \approx \frac{22.5 - 12}{1.5} \approx 7 \text{ k}\Omega$$

$$R_e \approx 7 - R_C \approx 7 - 5.6 \approx 1.4 \text{ k}\Omega$$

$$S \approx 1 \approx \beta \frac{1 \approx \frac{R_b}{R_e}}{1 \approx \beta \frac{R_b}{R_e}} \approx 3 \approx 1 \approx 50 \approx \frac{1 \approx \frac{R_b}{R_e}}{1 \approx 50 \approx \frac{R_b}{R_e}}$$



From this $\frac{R_b}{R_e} \approx 2.9 \text{ k}\Omega$, S will be < 3

$$I_B \approx \frac{I_C}{\beta} \approx \frac{1.5 \text{ mA}}{\beta} \approx \frac{1.5 \text{ mA}}{50} \approx 30 \mu\text{A}$$

Use equivalent circuit $R_b \approx R_1 \parallel R_2$

$$V_{Th} \approx V_{CC} \frac{R_2}{R_1 + R_2} \quad \text{or} \quad R_1 \approx R_b \frac{V_{CC}}{V_{Th}} \quad R_2 \approx R_1 \frac{V_{Th}}{V_{CC} - V_{Th}}$$

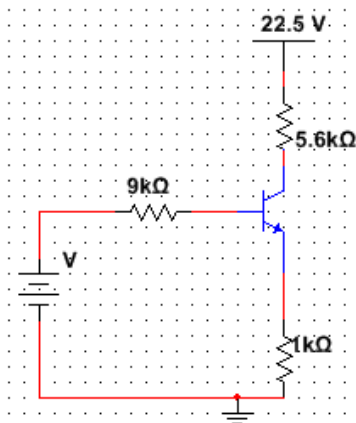
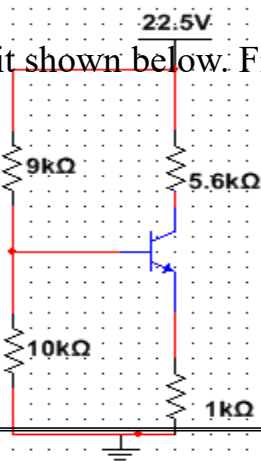
$$V \approx 30 \times 10^{-3} \times 2 - 90 \approx 0.6 \approx 3 \times 10^{-3} \approx 1.5 \approx 1.4 \approx 2.83 \text{ V}$$

$$R_1 \approx 2.96 \frac{22.5}{2.83} \approx 23.6 \text{ k}\Omega$$

$$R_2 \approx 23.6 \frac{2.83}{22.5 - 2.83} \approx 3.38 \text{ k}\Omega$$

Example:

For the circuit shown below. Find Q-point & S



≡

Solution:

$$V = \frac{22.5 \times 10}{90 \times 10} = 2.25 \text{ V} = V_2$$

$$R_b = \frac{10 \times 90}{10 \times 90} = 9 \text{ k}$$

Let $V_{BE} = 0.6 \text{ V}$

$$V_{CC} = I_C R_C + R_e (I_C + I_B) = V_{CE}$$

For collector circuit

$$22.5 = 5.6 I_C + 1 (I_C + I_B) = V_{CE}$$

For base circuit

$$2.25 = 0.6 + 1k (I_C + I_B) = 9 I_B$$

Eliminate I_C from these two equations

$$V_{CE} = 65 I_B = 11.6 \text{ i t ' s called biasing line}$$

Q-point is $V_{CE} = 12 \text{ V}$

$$I_C = 1.4 \text{ mA}$$

$$I_B = 26 \mu\text{A}$$

Alternatively, if dc in not available, one can do calculation from β . At active region

$$I_B \gg I_{Co}, \text{ so } I_C = \beta I_B$$

$$I_C = \beta (I_C + I_{Co}) = \beta I_C + \beta I_{Co}$$

$$I_B = \frac{I_C}{\beta} = \frac{I_C}{55} \quad \text{and from base equation}$$

$$.25 = 0.6 + 1k(I_C = I_B \cdot 9 = 9 I_B)$$

$$.25 = 0.6 + 1k(I_C = \frac{I_C}{55} \cdot 9 = 9 \frac{I_C}{55})$$

$$\therefore I_C = 1.4 \text{ mA}$$

$$I_B = \frac{1.4 \text{ mA}}{55} = 25.5 \mu\text{A}$$

These values are very close to these found from dc. From collector equation, can find V_{CE} .

$$-22.5 + 6.6 \cdot 1.4 = 25.5 \cdot 10^{-3} \cdot V_{CE}$$

$$\therefore V_{CE} = 13.2 \text{ V}$$

b)

$$\frac{R_b}{R_e} = \frac{9k}{1k} = 9$$

$$S = 56 \left(\frac{1}{56} \cdot 9 \right) = 8.61$$

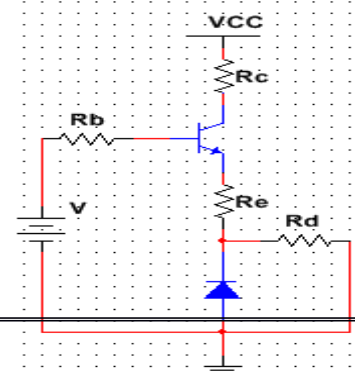
Compare with fixed bias circuit

$$S = \beta + 1 = 55 + 1 = 56$$

Bias Compensation:

There is loss in gain in earlier discussed techniques. The bias compensation techniques are used to reduce drift of Q.

Diode Compensation for V_{BE} :



If diode (D) and BE junction is with same material then the junction across diode has same temperature coefficient ($-2.5\text{mV}/^{\circ}\text{C}$) and the BE junction voltage V_{BE} .

If $T \uparrow \Rightarrow I_C \uparrow \Rightarrow I_E \uparrow$

$\downarrow I_D \Rightarrow I_E \Rightarrow I_{R_d}$

$I_{R_d} \rightarrow \text{const.}$

Exercises

1. Derive a mathematical expression to determine the stability factor

$S_{V_{CC}} \Delta I_C \Delta V_{CC}$ for the emitter-stabilized bias circuit.

2. Discuss and compare (by equations) between the relative levels of stability for the following biasing circuits:

- i. the fixed-bias circuit,
- ii. the emitter-stabilized bias circuit,
- iii. the voltage-divider bias circuit, and
- iv. the voltage-feedback circuit